

**Amendment to the Claims:**

This listing of claims will replace all prior versions, and listings, of claims in the application:

**Listing of Claims:**

1. (canceled)

2. (currently amended) A method of implementing an elliptic curve cryptographic operation in ~~an~~ a cryptographic apparatus implementing an elliptic curve cryptography in a finite field of characteristic 2 (or an extension field of "2"), in which said elliptic curve is given by  $y^2 + xy = ax^2 + b$  and in which  $x$  and  $y$  are variables in an  $x$ - $y$  coordinate system,  $a$  and  $b$  are parameters, addition of points  $P1$  ( $x1, y1$ ) and  $P2$  ( $x2, y2$ ) on said elliptic curve composed of points defined by individual coordinate components is presumed to be represented by  $P3$  ( $x3, y3$ ) with subtraction of said points  $P1$  ( $x1, y1$ ) and  $P2$  ( $x2, y2$ ) being presumed to be represented by  $P4$  ( $x4, y4$ ), said method comprising the steps performed by said cryptographic apparatus, of:

inputting the coordinate component  $x1$ ;

transforming ~~said the~~ inputted coordinate component  $x1$  into  $x$ -coordinates and  $z$ -coordinates  $[X_1, Z_1]$  of a projective space where  $z$  is a variable of a projective space where  $z$  is a variable in the  $z$ -coordinate;

storing said coordinates  $[X_1, Z_1]$  of said projective space;

transforming ~~said the~~ coordinate component  $x2$  into coordinates  $[X_2, Z_2]$  of said projective space;

storing ~~said the~~ projective coordinates  $[X_2, Z_2]$ ;  
transforming ~~said the~~ coordinate component  $x_4$  into coordinates  $[X_4, Z_4]$  of  
said projective space;  
storing ~~said the~~ coordinates  $[X_4, Z_4]$ ;  
determining projective coordinates  $[X_3, Z_3]$  from ~~said the~~ stored projective  
coordinates  $[X_1, Z_1]$ ,  $[X_2, Z_2]$  and  $[X_4, Z_4]$ ;  
transforming said projective coordinates  $[X_3, Z_3]$  into ~~said the~~ coordinate  
component  $x_3$ ; and  
outputting said coordinate component  $x_3$ ,  
whereby scalar multiplication of said point  $P1 (x_1, y_1)$  is determined;  
generating a random number  $k$ ;  
storing said generated random number  $k$ ;  
transforming the  $x$ - coordinates into projective coordinates to thereby derive  
projective coordinates  $[k^2x, k]$  through arithmetic operation of individual coordinate  
components of said projective space and said stored random number  $k$ .

3. (currently amended) A method of implementing an elliptic curve  
cryptographic operation in ~~an a cryptographic~~ apparatus implementing an elliptic  
curve cryptography in a finite field of characteristic 2 (or an extension field of "2"), in  
which said elliptic curve is given by  $y^2 + xy = ax^2 + b$  and in which  $x$  and  $y$  are  
variables in an  $x$ - $y$  coordinate system,  $a$  and  $b$  are parameters, addition of points  $P1$   
( $x_1, y_1$ ) and  $P2 (x_2, y_2)$  on said elliptic curve composed of points defined by  
individual coordinate components is presumed to be represented by  $P3 (x_3, y_3)$  with

subtraction of said points P1 ( $x_1, y_1$ ) and P2 ( $x_2, y_2$ ) being presumed to be represented by P4 ( $x_4, y_4$ ), said method comprising the steps performed by said cryptographic apparatus, of:

inputting the coordinate component  $x_1$ ;

transforming ~~said~~ the inputted coordinate component  $x_1$  into  $x$ - and  $z$ -coordinates [ $X_1, Z_1$ ] of a projective space where  $z$  is a variable of a projective space where  $z$  is a variable in the  $z$ -coordinate;

storing said coordinates [ $X_1, Z_1$ ] of said projective space;

transforming ~~said~~ the coordinate component  $x_2$  into coordinates [ $X_2, Z_2$ ] of said projective space;

storing ~~said~~ the projective coordinates [ $X_2, Z_2$ ];

transforming ~~said~~ the coordinate component  $x_4$  into coordinates [ $X_4, Z_4$ ] of said projective space;

storing ~~said~~ the coordinates [ $X_4, Z_4$ ];

determining projective coordinates [ $X_3, Z_3$ ] from ~~said~~ the stored projective coordinates [ $X_1, Z_1$ ], [ $X_2, Z_2$ ] and [ $X_4, Z_4$ ];

transforming ~~said~~ the projective coordinates [ $X_3, Z_3$ ] into said coordinate component  $x_3$ ; and

outputting said coordinate component  $x_3$ ,

whereby scalar multiplication of said point P1 ( $x_1, y_1$ ) is determined;

generating a random number  $k$ ;

storing said generated random number  $k$ ;

transforming the  $x$ - coordinates into projective coordinates to thereby derive projective coordinates  $[kx, k]$  through arithmetic operation of individual coordinate components of said projective space and said stored random number  $k$ .

4. - 5. (canceled)

6. (previously presented) An apparatus implementing an elliptic curve cryptographic operation in a finite field of characteristic 2 (or an extension field of "2"), in which  $x$  and  $y$  are variables in an  $x$ - $y$  coordinate system,  $a$  and  $b$  are parameters, said elliptic curve is given by  $y^2 + xy = x^3 + ax^2 + b$ , comprising:

random number generating means for generating a random number  $k$ ;

projective coordinate transformation means receiving as inputs thereto coordinate  $x_0$  of said finite field of characteristic 2 and said random number  $k$ , to thereby transform said coordinate  $x_0$  into projective coordinates  $[kx_0, k] = [X_1, Z_1]$ ;

doubling arithmetic means for arithmetically determining a double point from said projective coordinates  $[X_1, Z_1]$ ;

addition arithmetic means for determining an addition point from said projective coordinate  $[X_1, Z_1]$  where  $Z$  is a variable in the  $z$ -coordinate to thereby output said addition point; and

scalar multiplication means receiving information from said projective coordinate transformation means, said doubling arithmetic means and said addition arithmetic means to thereby perform scalar multiplication of the coordinate component  $x_0$ .

7. (canceled)

8. (currently amended) A recording medium storing a program for implementing an elliptic curve cryptographic operation, said recording medium being in ~~an~~ a cryptographic apparatus implementing an elliptic curve cryptography in a finite field of characteristic 2 (or an extension field of "2"), in which said elliptic curve is given by  $y^2 + xy = x^3 + ax^2 + b$ , in which  $x$  and  $y$  are variables in an  $x$ - $y$  coordinate system,  $a$  and  $b$  are parameters, addition of points  $P1 (x1, y1)$  and  $P2 (x2, y2)$  on said elliptic curve composed of points defined by individual coordinate components is presumed to be represented by  $P3 (x3, y3)$  with subtraction of points  $P1 (x1, y1)$  and  $P2 (x2, y2)$  being presumed to be represented by  $P4, (x4, y4)$ , said program when executed causing the cryptographic apparatus to perform:

inputting an coordinate component  $x1$ ;

transforming ~~said the~~ inputted coordinate component  $x1$  into  $x$ - and  $z$ -coordinates  $[X_1, Z_1]$  in a projective space;

storing said coordinates  $[X_2, Z_2]$  of said projective space;

transforming ~~said the~~ coordinate component  $x2$  into coordinates  $[X_2, Z_2]$  of said projective space;

storing ~~said the~~ projective coordinate  $[X_1, Z_1]$  where  $z$  is a variable in the  $z$ -coordinate;

transforming ~~said the~~ coordinate component  $x4$  into coordinates  $[X_4, Z_4]$  of said projective space;

storing ~~said the~~ projective coordinates  $[X_4, Z_4]$ ;  
determining projective coordinates  $[X_3, Z_3]$  from ~~said the~~ stored projective coordinates  $[X_1, Z_1]$ ,  $[X_2, Z_2]$  and  $[X_4, Z_4]$ ;  
transforming said projective coordinates  $[X_3, Z_3]$  into ~~said the~~ coordinate component  $x_3$ ; and  
outputting said coordinate component  $x_3$ ,  
whereby scalar multiplication of said point  $P_1 (x_1, y_1)$  is determined;  
generating a random number  $k$ ;  
storing said generated random number  $k$ ;  
transforming the  $x$ - coordinates into projective coordinates to thereby derive projective coordinates  $[k^2x, k]$  through arithmetic operation of individual coordinate components of said projective space and said stored random number  $k$ .

9. (currently amended) A recording medium storing a program for implementing an elliptic curve cryptographic operation, said recording medium being in ~~an a~~ cryptographic apparatus implementing an elliptic curve cryptography in a finite field of characteristic 2 (or an extension field of "2"), in which said elliptic curve is given by  $y^2 + xy = x^3 + ax^2 + b$ , in which  $x$  and  $y$  are variables in an  $x$ - $y$  coordinate system,  $a$  and  $b$  are parameters, addition of points  $P_1 (x_1, y_1)$  and  $P_2 (x_2, y_2)$  on said elliptic curve composed of points defined by individual coordinate components is presumed to be represented by  $P_3 (x_3, y_3)$  with subtraction of points  $P_1 (x_1, y_1)$  and  $P_2 (x_2, y_2)$  being presumed to be represented by  $P_4, (x_4, y_4)$ , said program when executed causing the cryptographic apparatus to perform:

inputting an coordinate component  $x_1$ ;

transforming ~~said-the~~ inputted coordinate component  $x_1$  into x- and z-coordinates  $[X_1, Z_1]$  in a projective space;

storing said coordinates  $[X_2, Z_2]$  of said projective space;

transforming ~~said-the~~ coordinate component  $x_2$  into coordinates  $[X_2, Z_2]$  of said projective space;

storing ~~said-the~~ projective coordinate  $[X_1, Z_1]$  where  $z$  is a variable in the z-coordinate;

transforming ~~said-the~~ coordinate component  $x_4$  into coordinates  $[X_4, Z_4]$  of said projective space;

storing ~~said-the~~ projective coordinates  $[X_4, Z_4]$ ;

determining projective coordinates  $[X_3, Z_3]$  from ~~said-the~~ stored projective coordinates  $[X_1, Z_1]$ ,  $[X_2, Z_2]$  and  $[X_4, Z_4]$ ;

transforming said projective coordinates  $[X_3, Z_3]$  into ~~said-the~~ coordinate component  $x_3$ ; and

outputting said coordinate component  $x_3$ ,

whereby scalar multiplication of said point  $P_1 (x_1, y_1)$  is determined;

generating a random number  $k$ ;

storing said generated random number  $k$ ;

transforming the x- coordinates into projective coordinates to thereby derive projective coordinates  $[kx, k]$  through arithmetic operation of individual coordinate components of said projective space and said stored random number  $k$ .

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10. - 12. (canceled)